## Search for Supersymmetry with Gauge-Mediated Breaking in Diphoton Events with Missing Transverse Energy at CDF II

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We present the results of a search for supersymmetry with gauge-mediated breaking and  $\widetilde{\chi}_1^0 \to \gamma \widetilde{G}$  in the  $\gamma\gamma+$ missing transverse energy final state. In 2.6±0.2 fb<sup>-1</sup> of  $p\bar{p}$  collisions at  $\sqrt{s}=1.96$  TeV recorded by the CDF II detector we observe no candidate events, consistent with a standard model background expectation of 1.4±0.4 events. We set limits on the cross section at the 95% C.L. and place the world's best limit of 149 GeV/c² on the  $\widetilde{\chi}_1^0$  mass at  $\tau_{\widetilde{\chi}_1^0}=0$  ns. We also exclude regions in the  $\widetilde{\chi}_1^0$  mass-lifetime plane for  $\tau_{\widetilde{\chi}_1^0}\lesssim 2$  ns.

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The standard model (SM) of elementary particles has 48 been enormously successful, but is incomplete. The- 49 oretical motivations [1] and the observation of the 50  $(ee\gamma\gamma + missing transverse energy (\cancel{E}_{T})'$  [2, 3] candidate 51 event by the CDF experiment during Run I at the Fer-52 milab Tevatron provide compelling rationale to search 53 for the production and decay of new heavy particles that 54 produce events with final state photons and  $E_{\rm T}$  in collider <sub>55</sub> experiments. Of particular theoretical interest are super-  $_{56}$ symmetry (SUSY) models with gauge-mediated SUSY-57 breaking (GMSB) [1]. These models solve the "natu- $_{58}$ ralness problem" [4] and provide a low-mass dark mat-59 ter candidate that is both consistent with inflation and  $_{60}$ astronomical observations [5]. Since many versions of these models have a similar phenomenology, we consider a scenario in which the lightest neutralino  $(\tilde{\chi}_1^0)$  decays almost exclusively (>96%) into a photon ( $\gamma$ ) and a weakly interacting, stable gravitino (G). The G gives rise to  $E_{\rm T}$  by leaving the detector without depositing any energy [6]. In these models, the  $\widetilde{\chi}_1^0$  is favored to have a lifetime on the order of a nanosecond, and the G is a warm dark matter candidate with a mass in the range  $0.5 < m_{\tilde{G}} < 1.5 \text{ keV}/c^2$  [7]. Other direct searches [8–10] have constrained the mass of the  $\tilde{\chi}_1^0$  to be greater than  $100 \text{ GeV/c}^2$  for much of the parameter space. At the Tevatron sparticle production is predicted to be primarily into gaugino pairs, and the  $\tilde{\chi}_1^0$  mass  $(m_{\tilde{\chi}_1^0})$  and lifetime  $(\tau_{\tilde{\chi}_1^0})$  are the two most important parameters in determining the final states and their kinematics [1]. Different search strategies are required for  $\widetilde{\chi}_1^0$  lifetimes above and  $^{^{76}}$ below about a nanosecond [11].

This Letter describes a search for GMSB, in which 79 gaugino pairs are produced and decay to the  $\gamma\gamma+\cancel{E}_T+X$  80 final state, where X denotes other high- $E_T$  final state 81 particles [12]. We use a dataset corresponding to an 82 integrated luminosity of  $2.6\pm0.2$  fb<sup>-1</sup> of  $p\bar{p}$  collisions 83 at  $\sqrt{s}$ =1.96 TeV from the Tevatron collected with the 84 CDF II detector [13]. This dataset is ten times larger 85 than the one used in our previous search [8]. For the 86 first time in this channel we use a new photon tim-87 ing system [14] and a new model of the  $\cancel{E}_T$  resolution 88 (METMODEL) [15]. These additions significantly enhance 89 our rejection of backgrounds from instrumental and non-90

collision sources, which allows us to considerably extend the sensitivity of the search for large  $\widetilde{\chi}_1^0$  masses compared to other Tevatron searches [9]. We also extend the search by considering  $\widetilde{\chi}_1^0$  lifetimes up to 2 ns which are favored for larger  $m_{\widetilde{\chi}^0}$ .

Our strategy is to select  $\gamma\gamma$  candidates and optimize the search for the presence of both significant  $E_T$  and large total event transverse energy to indicate the decays of heavy gauginos. We perform an *a priori* analysis based on the expected sensitivity, taking into account backgrounds from SM with mismeasured ("fake")  $E_T$ , electroweak production with real  $E_T$ , and non-collision sources and signal predictions.

Here we briefly describe the aspects of the detector [13] relevant to this analysis. The magnetic spectrometer consists of tracking devices inside a 3-m diameter, 5-m long superconducting solenoid magnet that operates at 1.4 T. A 3.1-m long drift chamber (COT) with 96 layers of sense wires measures the z position, time of the  $p\bar{p}$ interaction, and the momenta of charged particles. The calorimeter consists of projective towers with electromagnetic (EM) and hadronic (HAD) compartments and is divided into a central barrel that surrounds the solenoid coil ( $|\eta|<1.1$ ) [2] and a pair of end-plugs that cover the region  $1.1 < |\eta| < 3.6$ . The calorimeters are used to identify and measure the 4-momenta of photons, electrons, and jets (j) [16] and provide  $E_T$  information. The EM calorimeter is instrumented with a timing system, EM-Timing [14], that measures the arrival time of photons.

Our analysis begins with diphoton events passing the CDF three-level trigger. The combined trigger selection efficiency is effectively 100% if both photons have  $|\eta|<1.1$  and  $E_T>13$  GeV [12, 15]. Offline, both photons are required to be in the fiducial part of the calorimeter and to pass the standard CDF photon identification (ID) and isolation requirements [8], with two minor modifications to remove instrumental and electron backgrounds [15, 17]. The remaining events are dominated by SM production of  $\gamma\gamma$ ,  $\gamma j$  with  $j\rightarrow\gamma_{fake}$ , and  $jj\rightarrow\gamma_{fake}\gamma_{fake}$ , where  $\gamma_{fake}$  is a jet misidentified as a photon. To minimize the number of these events with large  $E_T$  due to calorimeter energy mismeasurements we remove events if the  $E_T$  vector points within  $|\Delta\phi|<0.3$ 

of the second highest  $E_{\rm T}$  photon or any jet pointing 56 to an uninstrumented region of the calorimeter [15]. 57 We require the primary collision vertex position with 58  $|z_{\rm vertex}| < 60$  cm in order to reduce non-collision back- 59 grounds and to maintain the projective nature of the 60 photon reconstruction in the calorimeter. For events with 61 multiple reconstructed vertices we recalculate the  $E_{\rm T}$ 's of 62 both photons and  $E_{\rm T}$  values if picking a different vertex 63 for them reduces the event  $E_{\rm T}$ .

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Non-collision backgrounds coming from cosmic rays 65 and beam-related effects can produce  $\gamma\gamma+\cancel{E}_{\rm T}$  candidates, 66 and are removed from the inclusive  $\gamma\gamma$  sample using a 67 number of techniques. Photon candidates from cosmic 68 rays are not correlated in time with collisions and events 69 are removed if the timing of either photon, corrected 70 for average path length  $(t_{\gamma})$ , indicates a non-collision 71 source [15, 17]. Photon candidates can also be produced 72 by beam-related muons that originate upstream of the 73 detector (from the more intense p beam). These are 74 suppressed using standard beam halo identification re-75 quirements [17]. A total of 38,053 inclusive  $\gamma\gamma$  candidate 76 events pass all the selection requirements.

Backgrounds to the  $\gamma\gamma + E_T$  final state from SM  $\gamma\gamma$ /78  $\gamma \gamma_{fake}/\gamma_{fake} \gamma_{fake}$  and fake  $E_T$  arise due to energy mis-79 measurements in the calorimeter or event reconstruction 80 pathologies. We use the METMODEL to select events 81 with real and significant  $E_{\rm T}$ , as part of the optimiza-82 tion, and to predict the contribution of SM backgrounds 83 with fake  $E_T$  due to normal energy measurement fluctu- 84 ations. This algorithm considers the clustered (jets) and 85 unclustered energy in the event and calculates a proba-86 bility for fluctuations in the energy measurement to pro- 87 duce  $E_T^{fluct}$  equivalent to or larger than the measured  $E_T$ , \*\*  $P_{E_T^{fluct} \geq E_T}$ . This probability is then used to define a  $E_{T}$ -89 significance as  $-\log_{10}\left(P_{\cancel{E}_{T}f^{luct} \geq \cancel{E}_{T}}\right)$ . Events with true  $_{91}^{90}$ and fake  $E_T$  of the same value have, on average, different 92  $E_{\text{T}}$ -significance. We use pseudo-experiments to estimate 93 the expected E<sub>T</sub>-significance distribution for SM events 94 with fake  $E_T$ , and the number of mismeasured events 95 above a given  $E_{T}$ -significance requirement. The jets and 96 unclustered energy are smeared according to their resolu-97 tion functions in the event. The systematic uncertainty 98 in the METMODEL is dominated by the uncertainty in the 99 resolution functions [15].

The METMODEL does not account for reconstruction<sup>101</sup> pathologies in SM events without intrinsic  $E_T$ , such as <sup>102</sup> a wrong choice of the primary interaction vertex or tri-<sup>103</sup> photon events with a lost photon. To obtain the pre-<sup>104</sup> diction for this background we model SM kinematics <sup>105</sup> and event reconstruction using a PYTHIA Monte Carlo <sup>106</sup> (MC) [18]  $\gamma\gamma$  sample that incorporates a detector simu-<sup>107</sup> lation [19]. Since the pathologies from  $\gamma j$  and jj sources <sup>108</sup> are similar in nature, but they are not included directly in <sup>109</sup> the simulation, we normalize to the number of events in <sup>110</sup> the inclusive  $\gamma\gamma$  data sample. We subtract the expecta-<sup>111</sup>

tions for energy mismeasurement fluctuations in the MC to avoid double counting. Uncertainties are dominated by the statistics of the MC sample.

Electroweak production of W and Z bosons which decay to leptons can also produce the  $\gamma\gamma + E_T$  signature where one or more of the photons can be fake, but the  $E_T$  is due to one or more neutrinos. To estimate the contribution from these backgrounds we use MC simulations, normalized to their theoretical cross sections and taking into account all the leptonic decay modes. The Baur MC [20] is used to simulate  $W\gamma$  and  $Z\gamma$  production and decay where initial and final state radiation (ISR/FSR) produce  $W/Z+\gamma\gamma$  events. The PYTHIA MC is used to simulate backgrounds where both photons are fakes: W and Z, with photons from ISR/FSR removed, and  $t\bar{t}$  sources. To minimize the dependence of our predictions on potential "MC-data" differences we scale our MC predictions to the observed number of  $e\gamma$  events [15] in data where we use the same diphoton triggers and analysis selection procedures used to select the inclusive  $\gamma\gamma$  sample. Uncertainties are dominated by the statistics of the MC and  $e\gamma$  normalization data sample.

Non-collision backgrounds are estimated using the data. Using the inclusive  $\gamma\gamma$  sample selection requirements, but requiring one of the photons to have  $t_{\gamma}{>}25$  ns we identify a cosmic-enhanced sample. Similarly, we utilize a beam-related background enhanced sample. We estimate the number of these events in the signal region using the ratio of events outside the timing requirements to events inside the signal region and the measured efficiencies of the non-collision rejection requirements [15]. The uncertainties on both non-collision background estimates are dominated by the statistical uncertainty on the number of identified events. Figure 1 (top) shows the  $E_T$ -significance distribution for the inclusive  $\gamma\gamma$  sample, along with the predictions for all the backgrounds.

We estimate the sensitivity to heavy, neutral particles that decay to photons using the GMSB reference model [6] in the mass-lifetime range,  $75 \le m_{\tilde{\chi}_1^0} \le 150$  GeV and  $\tau_{\tilde{\chi}_1^0} \lesssim 2$  ns. Events from all SUSY processes [21] are simulated with PYTHIA followed by a detector simulation. The fraction of  $\tilde{\chi}_1^0$  decays that occur in the detector volume, and thus the acceptance, are dependent on both the lifetime and the masses of the sparticles [11]. The total systematic uncertainty on the acceptance, after all kinematic requirements, is estimated to be 7%, dominated by the uncertainty in the photon ID efficiency (2.5% per photon). Other significant contributions come from uncertainties on ISR/FSR (4%), jet energy measurement (2%),  $E_T$ -significance parameterizations (1%) and parton distribution functions (1%).

We determine the final kinematic selection requirements by optimizing the mean expected 95% confidence level (C.L.) cross section limit using a no-signal assumption, before looking at the data in the signal region [22]. To compute the predicted cross section upper limit we

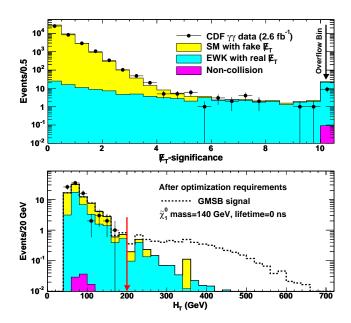


FIG. 1: The top plot shows the  $E_T$ -significance distribution for the inclusive  $\gamma\gamma$  candidate sample, along with the background predictions. The bottom plot shows the predicted  $H_T$  (total  $E_T$  of photons, jets, and  $E_T$ ) distribution after all but the final  $H_T$  requirement.

combine the luminosity, the acceptance and the background estimates with their systematic uncertainties using a Bayesian method [23]. The predicted limits are 31 optimized by simultaneously varying the selection re-32 quirements for  $E_{\rm T}$ -significance,  $H_{\rm T}$  (scalar sum of  $E_{\rm T}$  33 of photons, jets, and  $E_T$ ), and the azimuthal angle be-34 tween the two leading photons,  $\Delta \phi(\gamma_1, \gamma_2)$ . The large <sup>35</sup>  $E_{\mathrm{T}}$ -significance requirement eliminates most of the SM  $^{36}$ background with fake E<sub>T</sub>. GMSB production is domi- 37 nated by heavy gaugino pairs which decay to high- $E_{\mathrm{T}}$  38 light final state particles via cascade decays. The GMSB 39 signal has, on average, larger  $H_{\rm T}$  compared to SM back- 40 grounds so that an  $H_{\rm T}$  requirement can remove these 41 backgrounds effectively. Electroweak backgrounds with 42 large  $H_{\rm T}$  typically consist of a high- $E_{\rm T}$  photon recoil-43 ing against  $W \rightarrow e\nu$ , identified as  $\gamma_{fake} E_T$ , which means <sup>44</sup> the gauge boson decay is highly boosted. Thus, the two 45 photon candidates in the final state are mostly back-to-46 back. Also, the high- $E_{\rm T}$  diphotons with large  $H_T$  from 47 SM background are mostly back-to-back with fake  $E_T$ ; 48 the  $\Delta\phi(\gamma_1,\gamma_2)$  cut, therefore, reduces both these back-

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Each point in the considered  $\tau_{\tilde{\chi}_1^0}$  vs.  $m_{\tilde{\chi}_1^0}$  space gives 51 a slightly different optimization. We choose a single 52 set of requirements to maximize the region where the 53 predicted production cross section at next-to-leading or-54 der [24] is above the expected 95% C.L. cross section 55 limit. The exclusion region also takes into account the 56 production cross section uncertainties, which are domi-57 nated by the parton distribution functions (7%) and the 58

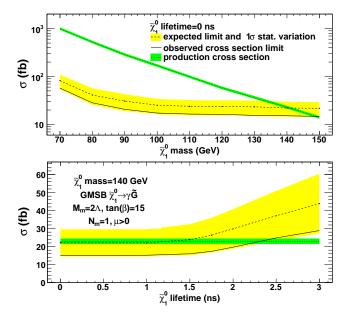
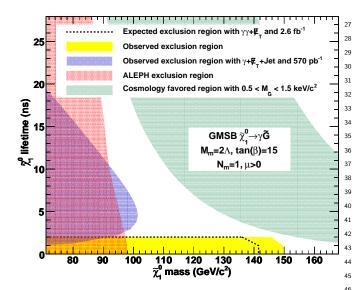


FIG. 2: The predicted and observed 95% C.L. cross section upper limits as a function of the  $\widetilde{\chi}^0_1$  mass at a lifetime of 0 ns (top) and as a function of the  $\widetilde{\chi}^0_1$  lifetime at a mass of 140 GeV/ $c^2$  (bottom). Indicated in green (darker shading) is the production cross section, along with its 8.0% uncertainty-band. In yellow (lighter shading) is the RMS variation on the expected cross section limit.

renormalization scale (3%). We find the optimal set of cuts, before unblinding the signal region, to be:  $E_{\rm T}$ -significance>3,  $H_{\rm T}$ >200 GeV, and  $\Delta\phi(\gamma_1,\gamma_2)<\pi-0.35$ . With these requirements we predict 1.4±0.4 background events, 0.9±0.4 of which is from electroweak sources (dominated by  $Z\gamma\gamma$  production) with real  $E_{\rm T}$ , 0.5±0.2 from SM with fake  $E_{\rm T}$ , and 0.001 $^{+0.008}_{-0.001}$  from non-collision sources. The acceptance for  $m_{\tilde{\chi}_1^0}$ =140 GeV/c² and  $\tau_{\tilde{\chi}_1^0}$ =0 ns is estimated to be 7.8±0.6%.

No events in the data pass the final event selection. The predicted  $H_{\rm T}$  distribution is shown in Figure 1 (bottom), after all but the final  $H_{\rm T}$  cut. The data is consistent with the no-signal hypothesis and is well modeled by SM backgrounds alone. We set cross section limits as a function of  $m_{\tilde{\chi}_1^0}$  and  $\tau_{\tilde{\chi}_1^0}$  respectively, as shown in Figure 2. The  $m_{\tilde{\chi}_1^0}$  reach, based on the predicted and observed number of events for  $\tau_{\tilde{\chi}_1^0}$ =0, is 141 GeV/c<sup>2</sup> and 149 GeV/c<sup>2</sup> respectively. These limits significantly extend the search sensitivity beyond the results of D0 [9], expand the results to include exclusions for  $\tau_{\tilde{\chi}_1^0} \leq 2$  ns, and, when combined with the complementary limits from CDF and LEP [10, 17], cover the region shown in Figure 3.

In conclusion, we have performed an optimized search for heavy, neutral particles that decay to photons in the  $\gamma\gamma+\cancel{E}_T$  final state using  $2.6\pm0.2~{\rm fb^{-1}}$  of data. There is no excess of events beyond expectations. We set cross section limits using a GMSB model with  $\widetilde{\chi}_1^0 \to \gamma \widetilde{G}$ , and



find an exclusion region in the  $\tau_{\tilde{\chi}_1^0}$ - $m_{\tilde{\chi}_1^0}$  plane with the  $_{57}^{50}$  world's best 95% C.L. lower limit on the  $\tilde{\chi}_1^0$  mass of  $_{58}^{58}$  149 GeV/c<sup>2</sup> at  $\tau_{\tilde{\chi}_1^0}$ =0 ns. By the end of Run II, with  $_{59}^{59}$  an integrated luminosity of 10 fb<sup>-1</sup>, we estimate a mass reach of  $\simeq 160$  GeV/c<sup>2</sup> at a lifetime of 0 ns.

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